

Higher Technological Institute
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Computer Graphics

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Lecture two

Graphics Output Primitives

OpenGL Point Functions

- The default color for primitives is white and the default point size is equal to the size of one screen pixel.
- The form for an OpenGL specification of a point position is

```
glBegin (GL_POINTS);
```

```
glVertex* ( );           //The coordinate values for a single position
```

```
glEnd ( );
```

- In the following example, three equally spaced points are plotted along a two-dimensional straight-line path with a slope of 2 (Figure). Coordinates are given as integer pairs.

```
glBegin (GL_POINTS);
```

```
glVertex2i (50, 100);
```

```
glVertex2i (75, 150);
```

```
glVertex2i (100, 200);
```

```
glEnd ( );
```

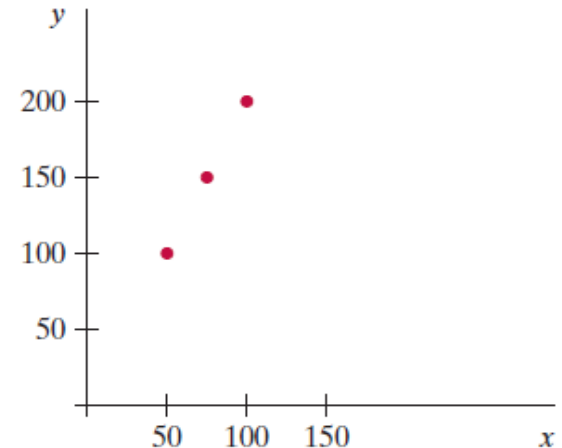


FIGURE Display of three point positions generated with `glBegin (GL_POINTS)`.

Alternatively, we could specify the coordinate values for the preceding points in arrays such as

```
int point1 [ ] = {50, 100};
```

```
int point2 [ ] = {75, 150};
```

```
int point3 [ ] = {100, 200};
```

and call the OpenGL functions for plotting the three points as

```
glBegin (GL_POINTS);
```

```
glVertex2iv (point1);
```

```
glVertex2iv (point2);
```

```
glVertex2iv (point3);
```

```
glEnd ( );
```

And here is an example of specifying two point positions in a three dimensional world reference frame. In this case, we give the coordinates as explicit floating-point values.

```
glBegin (GL_POINTS);
```

```
glVertex3f (-78.05, 909.72, 14.60);
```

```
glVertex3f (261.91, -5200.67, 188.33);
```

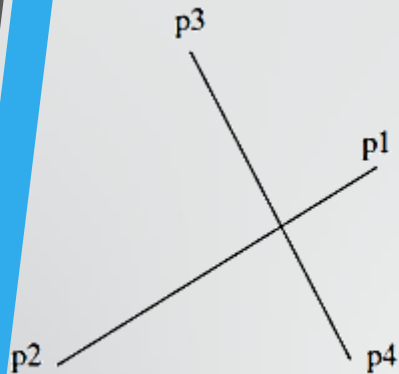
```
glEnd ( );
```

Using this class definition, we could specify two- dimensional, world-coordinate point position with the statements

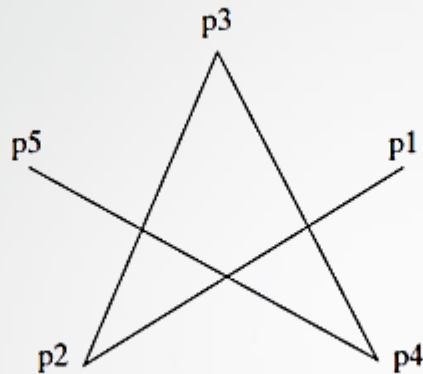
```
wcPt2D pointPos;  
pointPos.x = 120.75;  
pointPos.y = 45.30;  
glBegin (GL_POINTS);  
glVertex2f (pointPos.x, pointPos.y);  
glEnd ( );
```

**Look to pages in textbook "Computer Graphics with open GL"
Pages(88-89)**

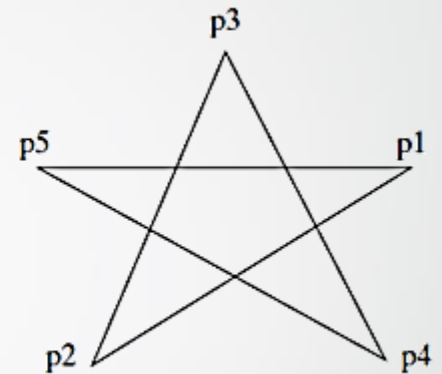
OpenGL LINE FUNCTIONS



(a)



(b)



(c)

The following code could generate the display shown in Figure.

```
glBegin (GL_LINES);  
glVertex2iv (p1);  
glVertex2iv (p2);  
glVertex2iv (p3);  
glVertex2iv (p4);  
glVertex2iv (p5);  
glEnd ( );
```

```
glBegin (GL_LINES_STRIP);  
glVertex2iv (p1);  
glVertex2iv (p2);  
glVertex2iv (p3);  
glVertex2iv (p4);  
glVertex2iv (p5);  
glEnd ( );
```

```
glBegin (GL_LINES_LOOP);  
glVertex2iv (p1);  
glVertex2iv (p2);  
glVertex2iv (p3);  
glVertex2iv (p4);  
glVertex2iv (p5);  
glEnd ( );
```

LINE-DRAWING ALGORITHMS

- A straight-line segment in a scene is defined by the coordinate positions for the endpoints of the segment.
- The line color is loaded into the frame buffer at the corresponding pixel coordinates.
- Stair-step effect (jaggies) produced when a line is generated as a series of pixel positions.



Line Equations

$$y = m \cdot x + b \quad (1)$$

$$m = \frac{y_{\text{end}} - y_0}{x_{\text{end}} - x_0} \quad (2)$$

$$b = y_0 - m \cdot x_0 \quad (3)$$

For any given x interval δx along a line, we can compute the corresponding δy interval δy from Eq. 2 as

The Cartesian *slope-intercept equation* for a straight line is

$$\delta y = m \cdot \delta x \quad (4)$$

$$\delta x = \frac{\delta y}{m} \quad (5)$$

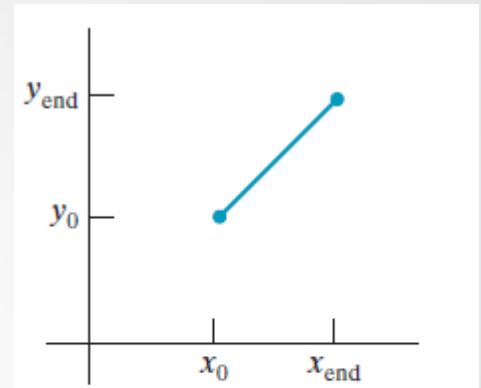


FIGURE Line path between endpoint positions (x_0, y_0) and $(x_{\text{end}}, y_{\text{end}})$.

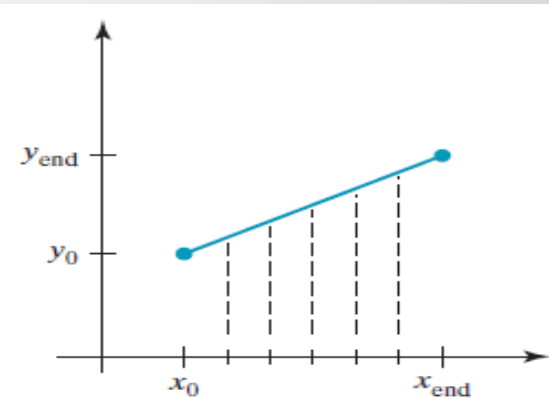


FIGURE Straight-line segment with five sampling positions along the x axis between x_0 and x_{end} .

The *Digital Differential Analyzer* (DDA)

We consider first a line with **positive** slope,

If the **slope is less than or equal to 1**, we sample at unit x intervals ($\delta x = 1$) and compute successive y values as

$$y_{k+1} = y_k + m \quad (6)$$

Subscript k takes integer values starting from 0, for the first point, and increases by 1 until the final endpoint is reached. Since m can be any real number between 0.0 and 1.0, each calculated y value must be rounded to the nearest integer corresponding to a screen pixel position in the x column we are processing.

For lines with **a positive slope greater than 1.0**, we reverse the roles of x and y .

That is, we sample at unit y intervals ($\delta y = 1$) and calculate consecutive x values as

$$x_{k+1} = x_k + \frac{1}{m} \quad (7)$$

In this case, each computed x value is rounded to the nearest pixel position along the current y scan line.

Equations 6 and 7 are based on the assumption that lines are to be processed from the left endpoint to the right endpoint

If this processing is **reversed**, so that the **starting endpoint is at the right**, then either we have $\delta x = -1$ and

$$y_{k+1} = y_k - m$$

or (when the **slope is greater than 1**) we have $\delta y = -1$ with

$$x_{k+1} = x_k - \frac{1}{m}$$

This algorithm is summarized in the following procedure, which accepts as input two integer screen positions for the endpoints of a line segment. **Horizontal and vertical differences between the endpoint positions are assigned to parameters \mathbf{dx} and \mathbf{dy} .** The difference with the greater magnitude determines the value of parameter **steps**. Starting with pixel position **($\mathbf{x_0}, \mathbf{y_0}$)**, we determine the offset needed at each step to generate the next pixel position along the line path. We loop through this process **steps** times. If the magnitude of \mathbf{dx} is greater than the magnitude of \mathbf{dy} and $\mathbf{x_0}$ is less than \mathbf{xEnd} , the values for the increments in the x and y directions are 1 and m , respectively. If the greater change is in the x direction, but $\mathbf{x_0}$ is greater than \mathbf{xEnd} , then the decrements -1 and $-m$ are used to generate each new point on the line. Otherwise, we use a unit increment (or decrement) in the y direction and an x increment $\frac{1}{m}$ (or decrement) of .

The *digital differential analyzer* (DDA) Algorithm: (textbook pg4)

The *digital differential analyzer* (DDA) is a scan-conversion line algorithm based on calculating either δx or δy , using Eq. 4 or Eq. 5.

```
#include <stdlib.h>
#include <math.h>

inline int round (const float a) { return int (a + 0.5); }

void lineDDA (int x0, int y0, int xEnd, int yEnd)
{
    int dx = xEnd - x0, dy = yEnd - y0, steps, k;
    float xIncrement, yIncrement, x = x0, y = y0;

    if (fabs (dx) > fabs (dy))
        steps = fabs (dx);
    else
        steps = fabs (dy);
    xIncrement = float (dx) / float (steps);
    yIncrement = float (dy) / float (steps);

    setPixel (round (x), round (y));
    for (k = 0; k < steps; k++) {
        x += xIncrement;
        y += yIncrement;
        setPixel (round (x), round (y));
    }
}
```

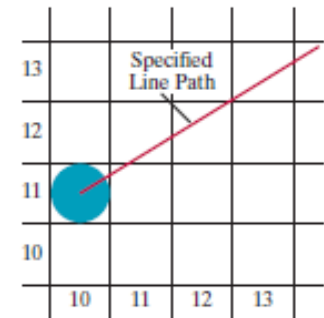


FIGURE 3-8 A section of a display screen where a straight-line segment is to be plotted, starting from the pixel at column 10 on scan line 11.

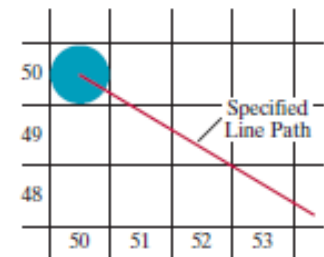


FIGURE 3-9 A section of a display screen where a negative slope line segment is to be plotted, starting from the pixel at column 50 on scan line 50.

EXAMPLE 1:

Apply The *digital differential analyzer* (DDA) Algorithm to compute which pixels should be turned on to represent the line from (2,2) to (8,7)

DDA- Digital Differential Analyser

This case is for slope (m) less than 1. Slope (m) = $(7-1)/(8-1) = 6/7$.

S-1: $x_1=1; y_1=1; x_2=8; y_2=7$.

S-2: $m=(7-1)/(8-1) = 6/7$ which is less than 1.

S-3: As m (6/7) is less than 1 therefore x is increased and y is calculated.

S-4: The step will be $x_1=x_1+1$ and $y_1 = y_1+6/7$

S-5: The points generated would be $x_1=1+1$ and $Y_1=1+(5/7) \Rightarrow 1+0.9 \Rightarrow 1.9 \Rightarrow$ approx 2. So $X_1=2$ and $Y_1=2$

	X1	Y1	Pixel Plotted
p1	2	2	2,2
p2	3	$2+6/7 = 2.9$	3,3
p3	4	$2.9 + 6/7 = 3.8$	4,4
p4	5	$3.8 + 6/7 = 4.7$	5,5
p5	6	$4.7 + 6/7 = 5.6$	6,6
p6	7	$5.6 + 6/7 = 7.0$	7,7

The algorithm will stop here as the x value has reached 7.

EXAMPLE 2:

Apply The *digital differential analyzer* (DDA) Algorithm to compute which pixels should be turned on to represent the line from (0,0) to (4,6)

This case is for slope (m) greater than 1. Slope (m) = $(6-0)/(4-0) = 6/4$.

S-1: $x_1=0; y_1=0; x_2=4; y_2=6$

S-2: $m=(6-0)/(4-0) = 6/4$ which is more than 1.

S-3: As m (6/4) is greater than 1 therefore y is increased and x is calculated.

S-4 : Now increase the value of y and calculate value of x.

- To calculate x, take line equation and find x , $x_2=x_1+1/m$
- The step will be $y_1=y_1+1$ and $x_1 =x_1+1/(6/4)$, After Simplification, Every time $y_1=y_1+1$ and $x_1=x_1+4/6$

	Y1	X1	Pixel Plotted
p0	0	0	(0,0)
p1	1	$x_1 = (0)+4/6=0.67 = 1$	(1,1)
p2	2	$0.67+4/6 = 1.34$	(1,2)
p3	3	$1.34+4/6=2.01$	(2,3)
p4	4	$2.01+4/6= 2.68$	(3,4)
p5	5	$2.68+4/6=3.35$	(3,5)
p6	6	$3.35+4/6=4.02$	(4,6)

EXAMPLE 3:

Apply The *digital differential analyzer* (DDA) Algorithm to compute which pixels should be turned on to represent the line from (2,3) to (9,8)

S-1: $x_1=2, y_1=3$ and $x_2=9, y_2=8$.

S-2: Calculate Slope $m = (8-3)/(9-2) = 5/7$, which is less than 1.

S-3: Since m is less than one that means we would increase x and calculate y .

S-4: So new x would be equal to old x plus 1 😊 and calculate y as new $y = \text{old } y + m(\text{slope})$. — Easy to understand. We mean the following

$x_1=x_1+1$ and $y_1=y_1+(5/7)$

	X1	Y1	Pixel Plotted
p0	2	3	2,3
p1	3	$3+5/7 \Rightarrow 26/7 \Rightarrow 26/7 \Rightarrow 3.71$	3,4
p2	4	$3.71 + 5/7 = 4.42$	4,4
p3	5	$4.42 + 5/7 = 5.13$	5,5
p4	6	$5.13 + 5/7 = 5.84$	6,6
p5	7	$5.84 + 5/7 = 6.55$	7,7
p6	8	$6.55+5/7=7.26$	8,7
p7	9	$7.26+5/7=7.97$	9,8

The algorithm would stop here as we have reached the end point of the line (9,8)

Exercise :

Apply The *digital differential analyzer* (DDA) Algorithm to compute which pixels should be turned on to represent the line from (20,10) to (30,18)

dx	dy	steps	k	X Increment	Y Increment	x	y	(x,y)
						20	10	(20,10)
10	8	10	0	1	0.8	21	10.8	(21,11)
			1			22	11.6	(22,12)
			2			23	12.3	(23,12)
			3			24	13.1	(24,13)
			4			25	13.9	(25,14)
			5			26	14.7	(26,15)
			6			27	15.5	(27,15)
			7			28	16.3	(28,16)
			8			29	17.1	(29,17)
			9			30	17.9	(30,18)

Bresenham's Line Algorithm

Bresenham's Line-Drawing Algorithm for $|m| < 1.0$

1. Input the two line endpoints and store the left endpoint in (x_0, y_0) .
2. Set the color for frame-buffer position (x_0, y_0) ; i.e., plot the first point.
3. Calculate the constants Δx , Δy , $2\Delta y$, and $2\Delta y - 2\Delta x$, and obtain the starting value for the decision parameter as

$$p_0 = 2\Delta y - \Delta x$$

4. At each x_k along the line, starting at $k = 0$, perform the following test. If $p_k < 0$, the next point to plot is $(x_k + 1, y_k)$ and

$$p_{k+1} = p_k + 2\Delta y$$

Otherwise, the next point to plot is $(x_k + 1, y_k + 1)$ and

$$p_{k+1} = p_k + 2\Delta y - 2\Delta x$$

5. Perform step 4 $\Delta x - 1$ times.

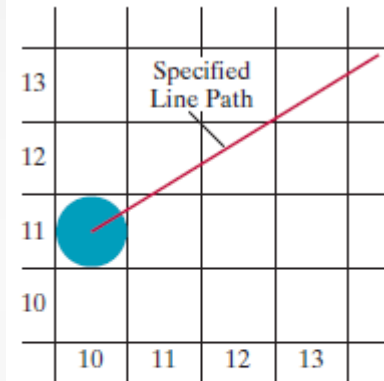


FIGURE A section of a display screen where a straight-line segment is to be plotted, starting from the pixel at column 10 on scan line 11.

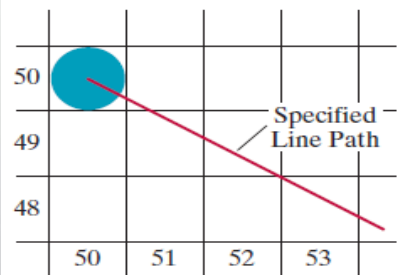


FIGURE A section of a display screen where a negative slope line segment is to be plotted, starting from the pixel at column 50 on scan line 50.

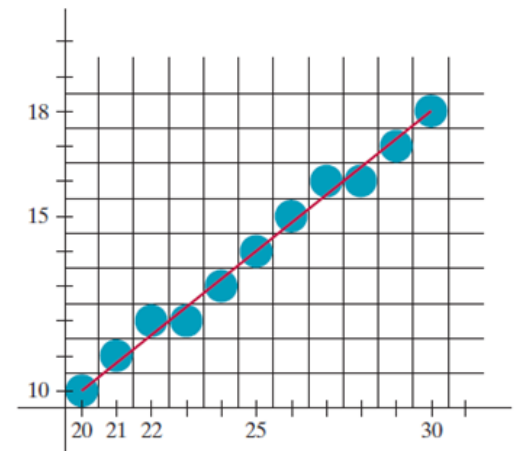
Bresenham's Line Algorithm

EXAMPLE :(textbook p136-137)

To illustrate the algorithm, we digitize the line with endpoints (20, 10) and (30, 18).

- Draw the line with endpoints (20,10) and (30, 18).
 - $\Delta x=30-20=10$, $\Delta y=18-10=8$,
 - $p_0 = 2\Delta y - \Delta x=16-10=6$
 - $2\Delta y=16$, and $2\Delta y - 2\Delta x=-4$
- Plot the initial position at (20,10), then

k	p_k	(x_{k+1}, y_{k+1})	k	p_k	(x_{k+1}, y_{k+1})
0	6	(21, 11)	5	6	(26, 15)
1	2	(22, 12)	6	2	(27, 16)
2	-2	(23, 12)	7	-2	(28, 16)
3	14	(24, 13)	8	14	(29, 17)
4	10	(25, 14)	9	10	(30, 18)



Bresenham's Line Algorithm

An implementation of Bresenham line drawing for slopes in the range $0 < m < 1.0$ is given in the following procedure

```
#include <stdlib.h>
#include <math.h>

/* Bresenham line-drawing procedure for |m| < 1.0. */
void lineBres (int x0, int y0, int xEnd, int yEnd)
{
    int dx = fabs (xEnd - x0),  dy = fabs(yEnd - y0);
    int p = 2 * dy - dx;
    int twoDy = 2 * dy,  twoDyMinusDx = 2 * (dy - dx);
    int x, y;

    /* Determine which endpoint to use as start position. */
    if (x0 > xEnd) {
        x = xEnd;
        y = yEnd;
        xEnd = x0;
    }
    else {
        x = x0;
        y = y0;
    }
    setPixel (x, y);

    while (x < xEnd) {
        x++;
        if (p < 0)
            p += twoDy;
        else {
            y++;
            p += twoDyMinusDx;
        }
        setPixel (x, y);
    }
}
```

End of Lecture Good Luck!

See you
in next lecture...

